

## **2nd International FLAC/DEM Symposium**

# **Lateral Earth Pressures with Layered Backfill**

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Senior Lecturer in Geotechnical Engineering

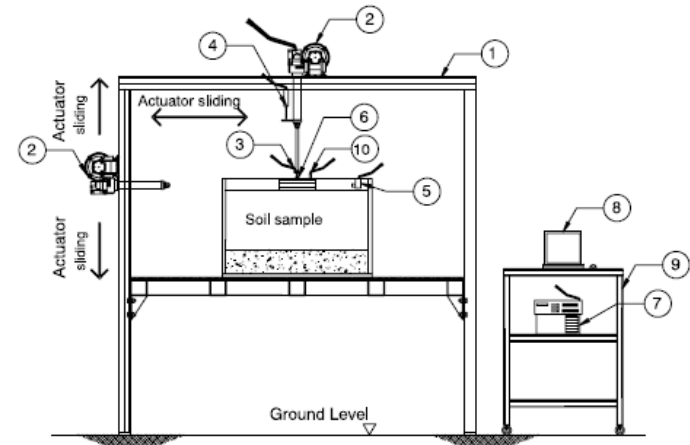
Faculty of Engineering and Surveying  
University of Southern Queensland  
Toowoomba, QLD, Australia

# USQ, Toowoomba, Queensland, Australia



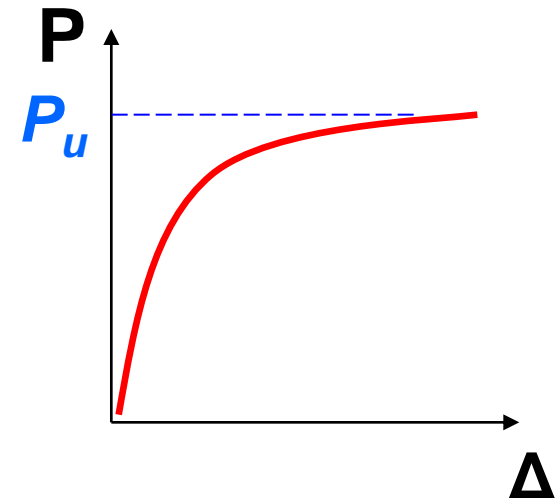
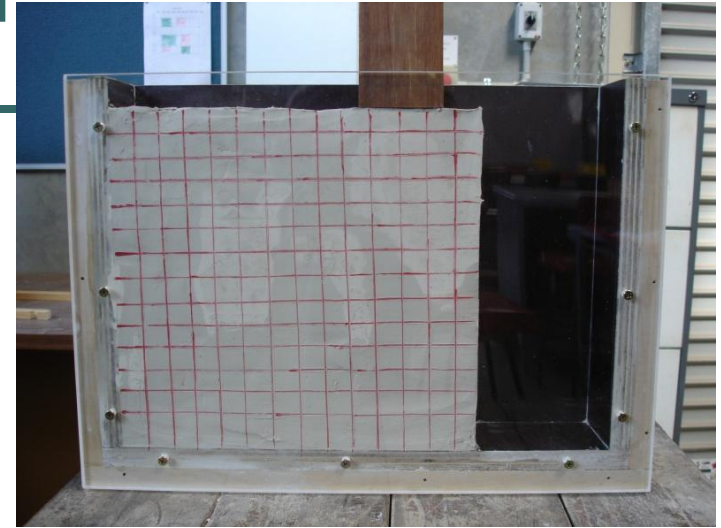
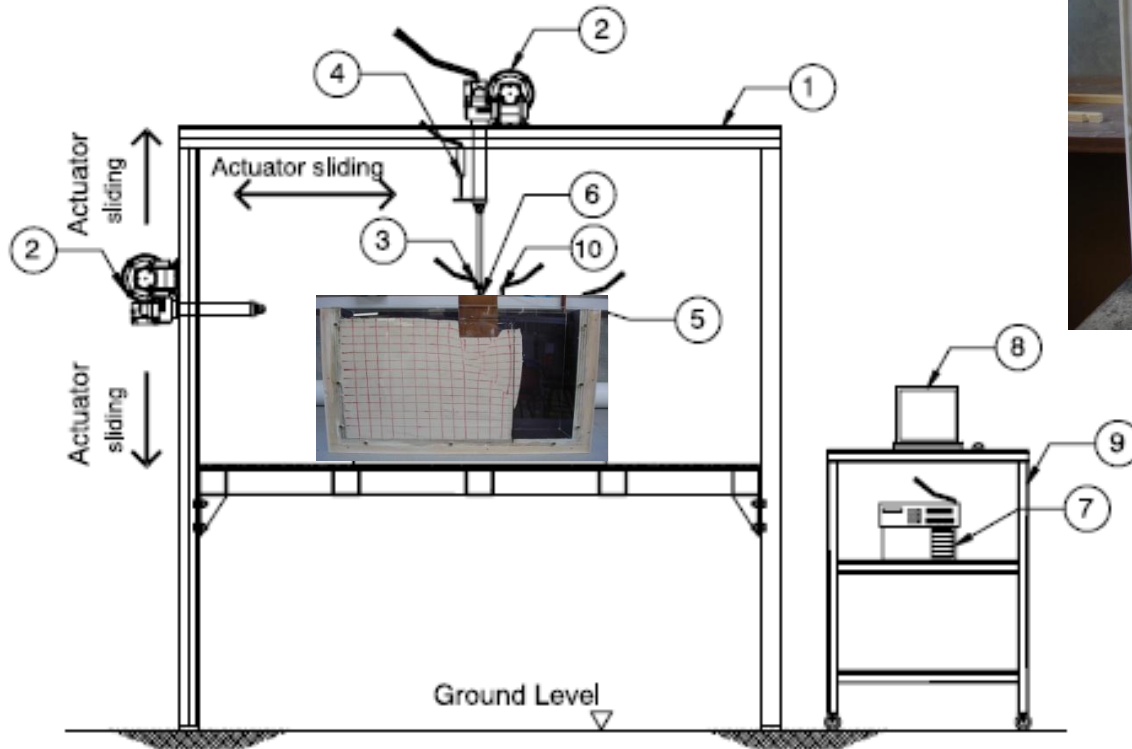
# Background to research

- To make use of the existing resources at USQ ( both 2D and 3D FLAC licences), we aim to develop numerical models for various geotechnical applications.
- Research at USQ also involves developing various physical models for teaching purposes, so as to complement the numerical approach using computer modeling.



# Background to research

## USQ Geotechnical Stability Testing Rigs





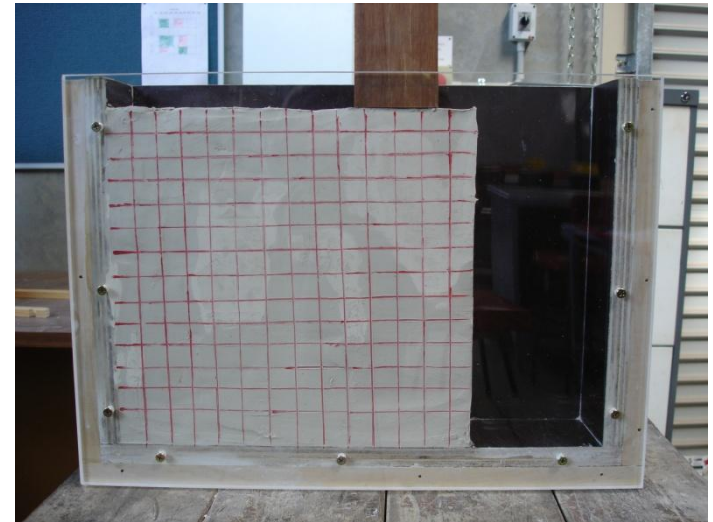
13 July 2011

Dr. Jim Shiau

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# What is physical model?

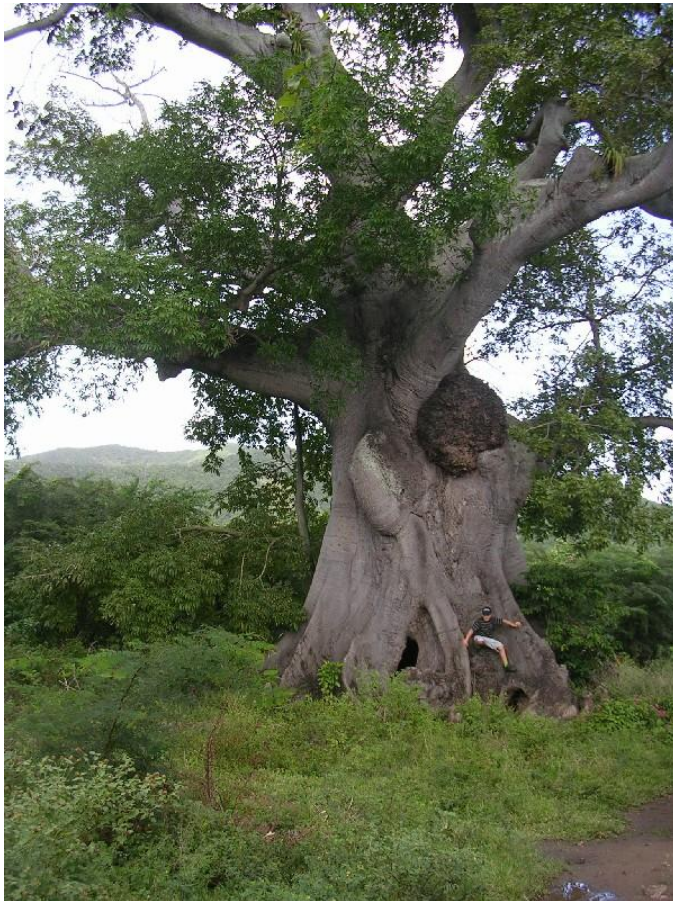
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A landslide model to simulate the failure pattern of a slope.

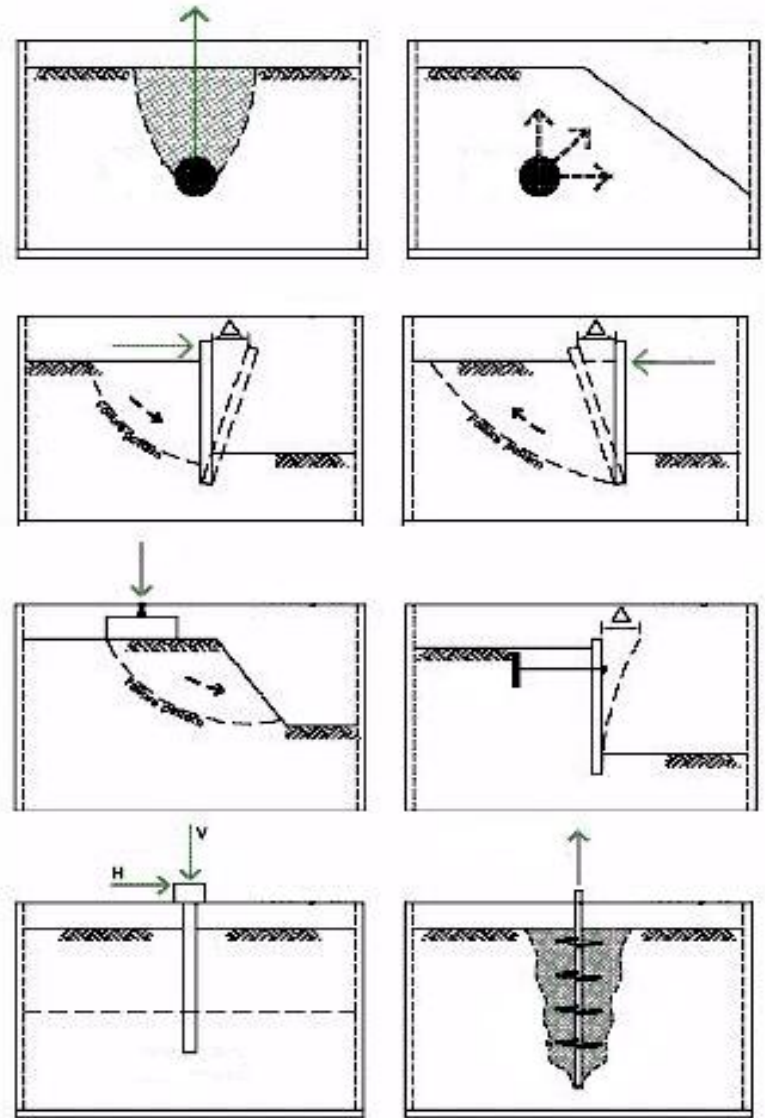
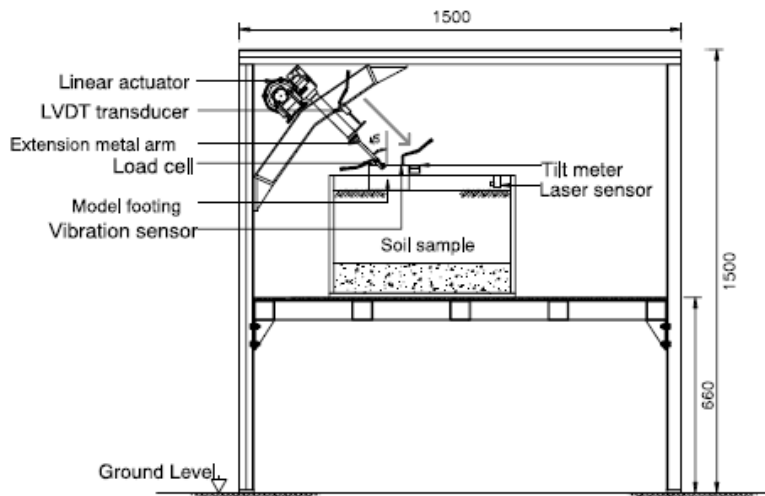
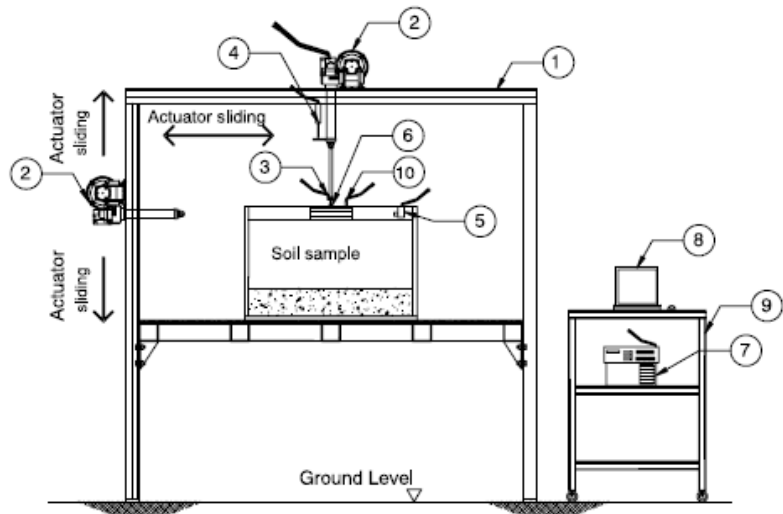
# Bonsai vs. Physical Model

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Bonsai

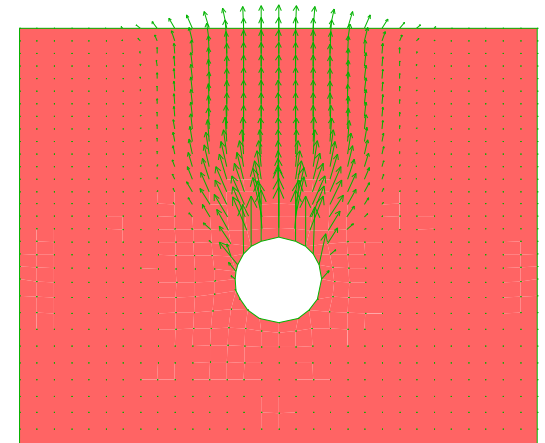
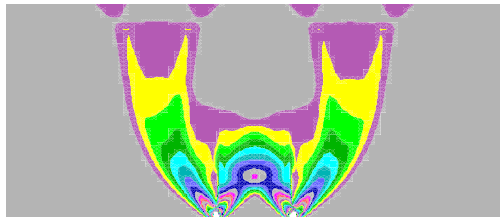
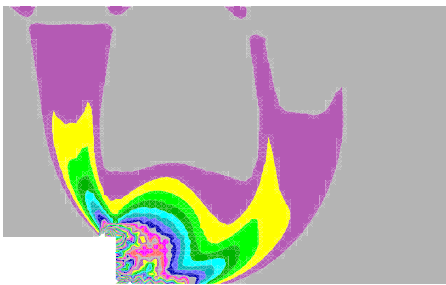
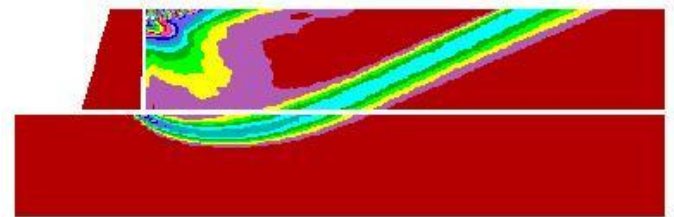
The knowledge gained in the process of Bonsai making would help to understand the behaviour of a real tree.





# Various Stability Models using FLAC

- Classical earth pressure problems
- Slotted wall
- Trapdoor
- Tunnel heading
- Uplift of buried pipe
- Uplift of ground anchor



# Background to research

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- **Had some experience in Upper and Lower Bound Limit Analyses during my stay in Newcastle Geotechnical Group during 1998-2003.**
- **Overall, my research interests at USQ**
  - To develop stability models using FLAC.
  - To develop stability models using Upper and Lower limit analyses.
  - Physical modeling using simple stability testing rigs at USQ.
- **Two papers in this symposium:**
  - Modeling Uplift of Plate Anchor
  - Earth Pressures with Layered Backfill

# Goal and Objective

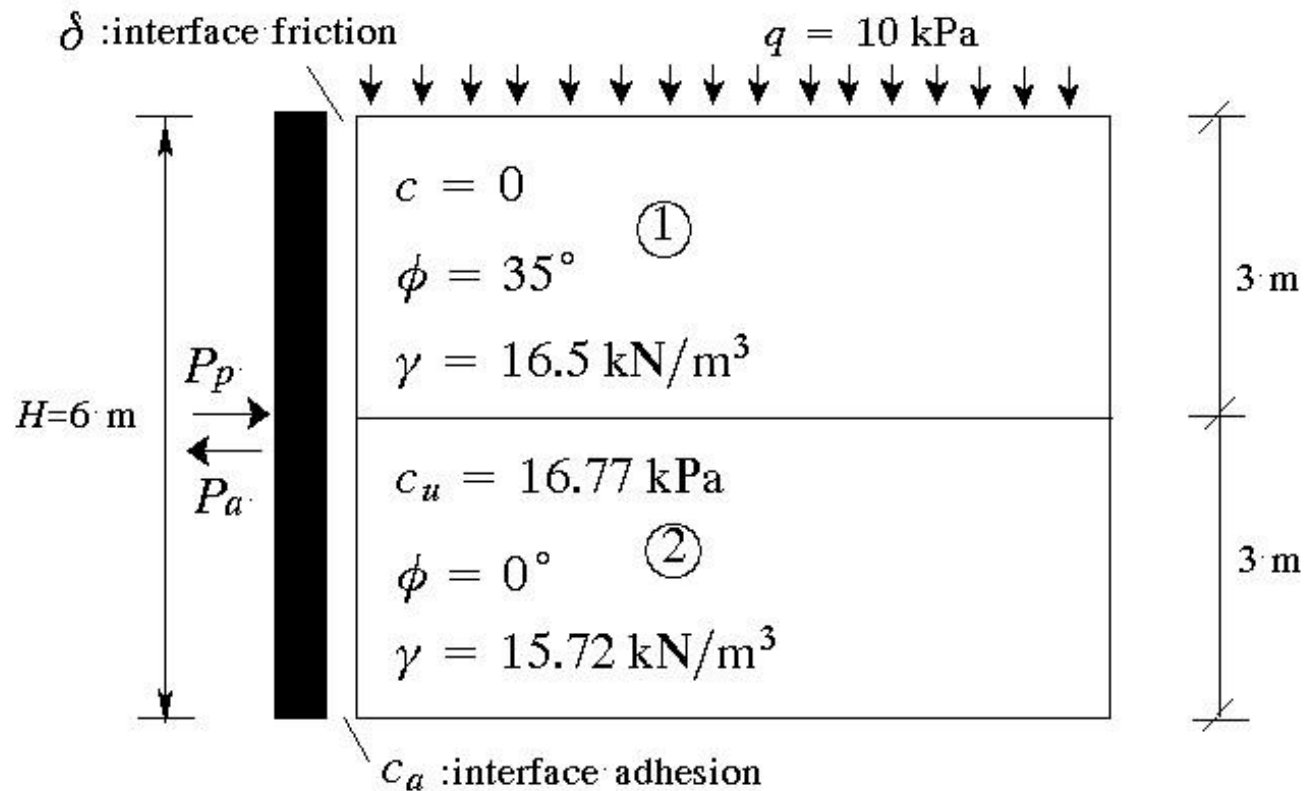
## *Lateral Earth Pressures with Layered Backfill*

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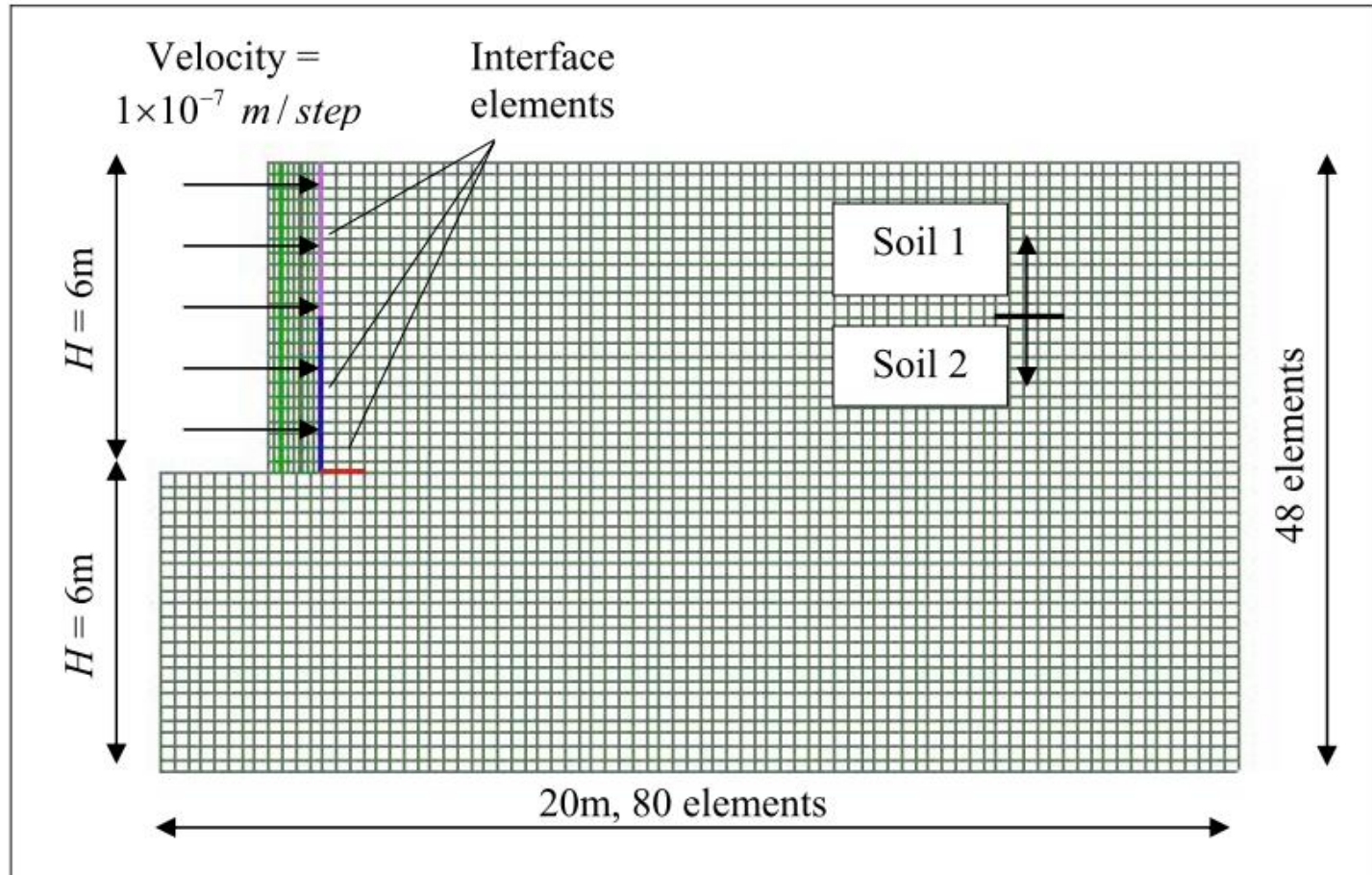
- To investigate the situation of active and passive earth pressures on the back of a retaining wall with layered backfill.
- To compare FLAC results with those using classical earth pressure theory and *FE Limit Analyses - Upper and Lower Limit Analyses*.
  - *FLAC*
  - *Rankine/Coulomb/Log Spiral*
  - *Upper and Lower bounds*

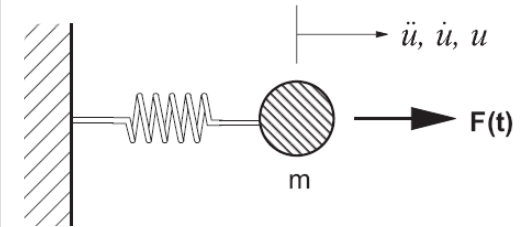
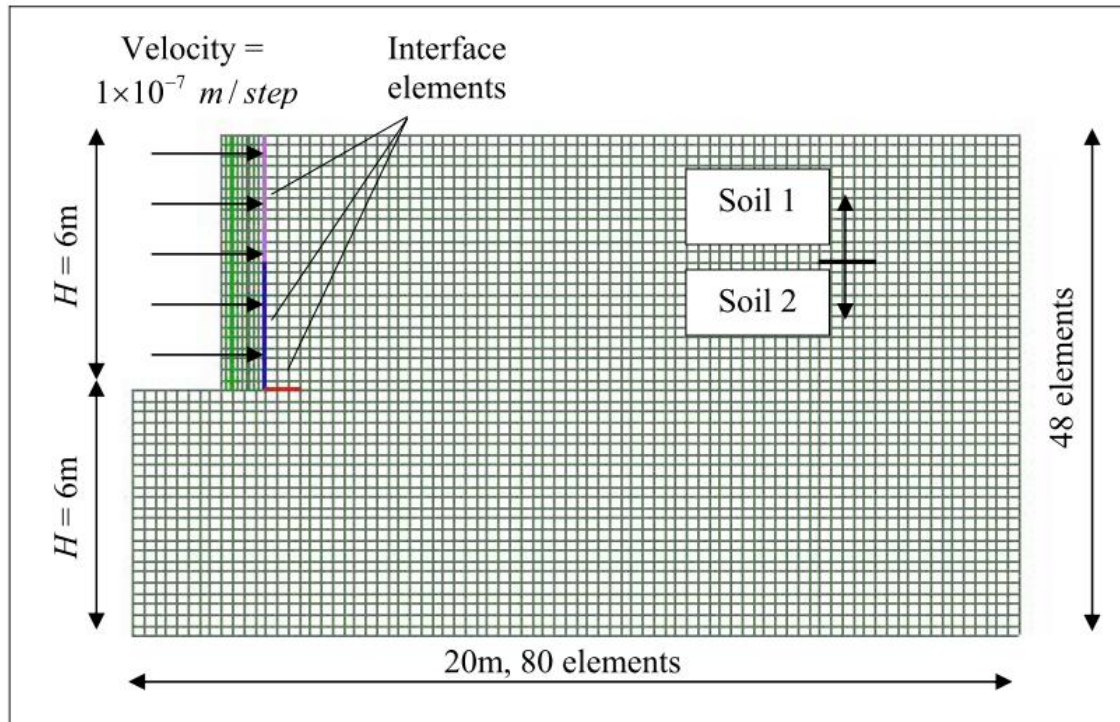
*For smooth and rough wall cases!*

# The problem definition



# The problem definition



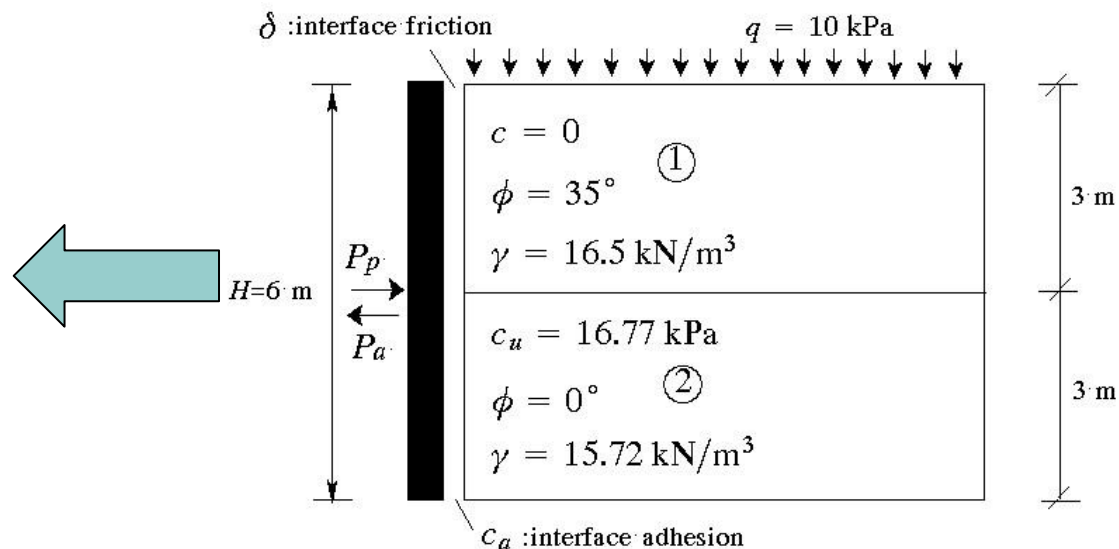


$$m \frac{d\dot{u}}{dt} = F$$

To solve a static system using the dynamic equation of motion, an artificial nodal damping is needed so that kinetic energy can be gradually removed.

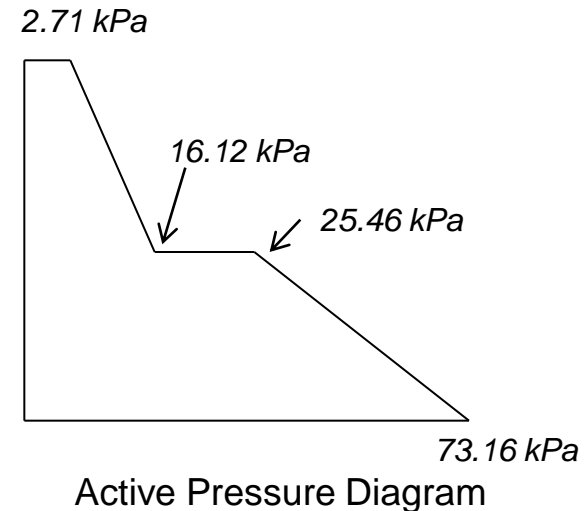
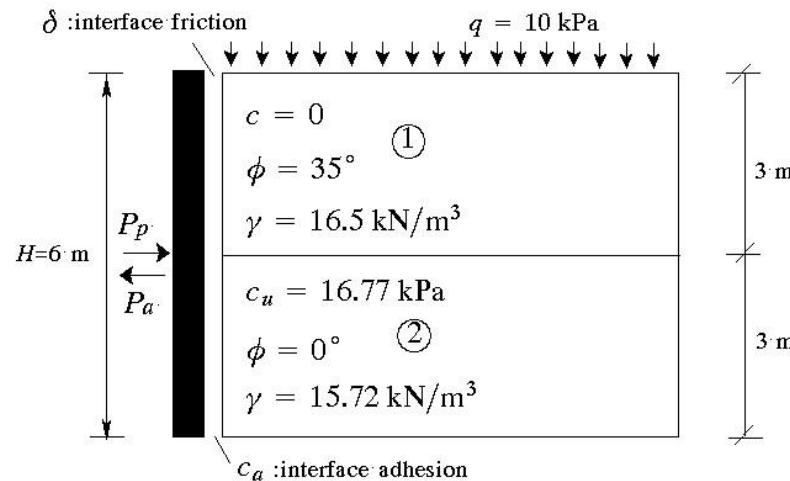
# Smooth case - Active wall

- FLAC solution
- Textbook solution – Rankine
- Upper and Lower bound solutions



# Textbook solution of the problem

Active wall – smooth wall case – Rankine’s solution



Rankine: Total horizontal active thrust = 176.18 kN/m  
 FLAC solution = 167.20 kN/m



# Upper and lower bound solutions of the problem

Active wall – smooth wall case

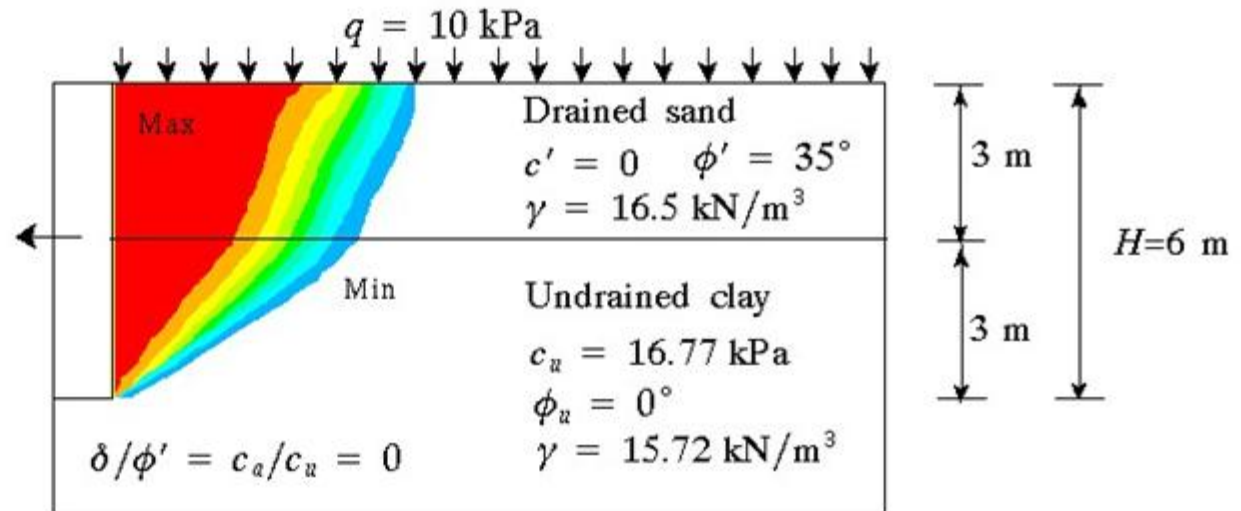
Smooth wall

$$(P_a)^{UB} = 166.35 \text{ kN/m}$$

$$(P_a)^{LB} = 173.21 \text{ kN/m}$$

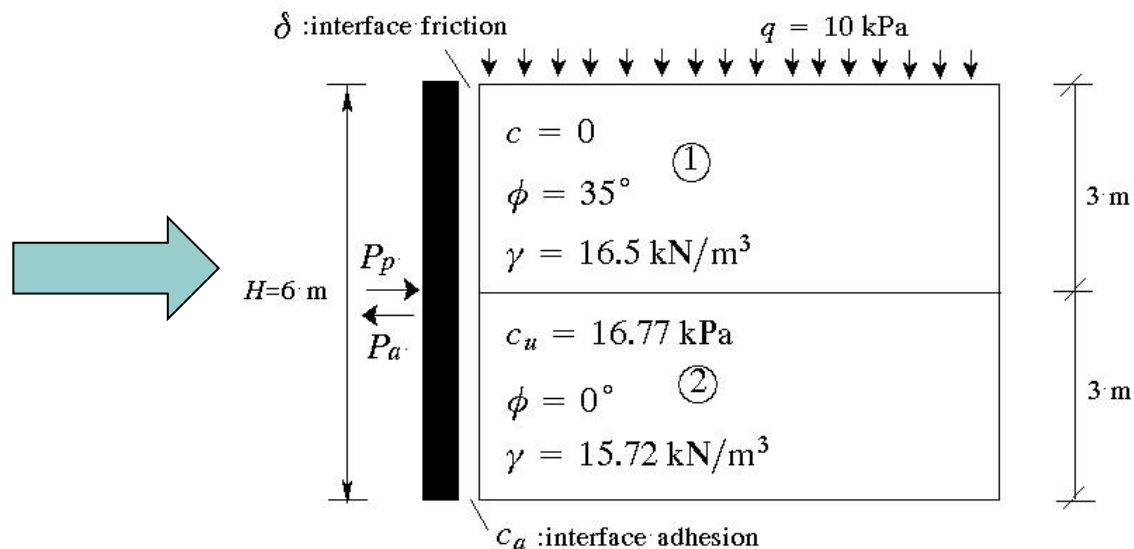
$$(P_a)^{Rankine} = 176.18 \text{ kN/m}$$

**FLAC solution**  
**= 167.20 kN/m**



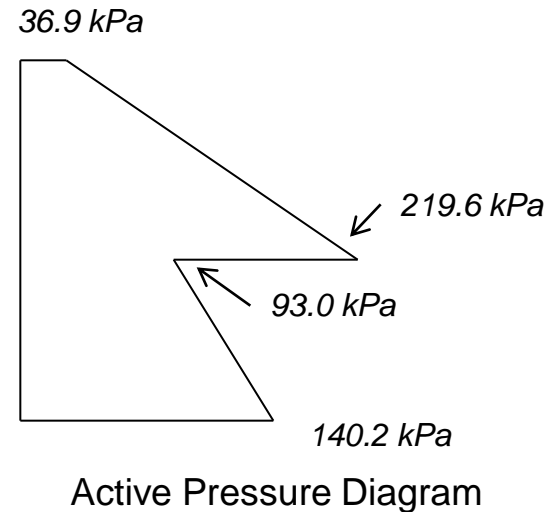
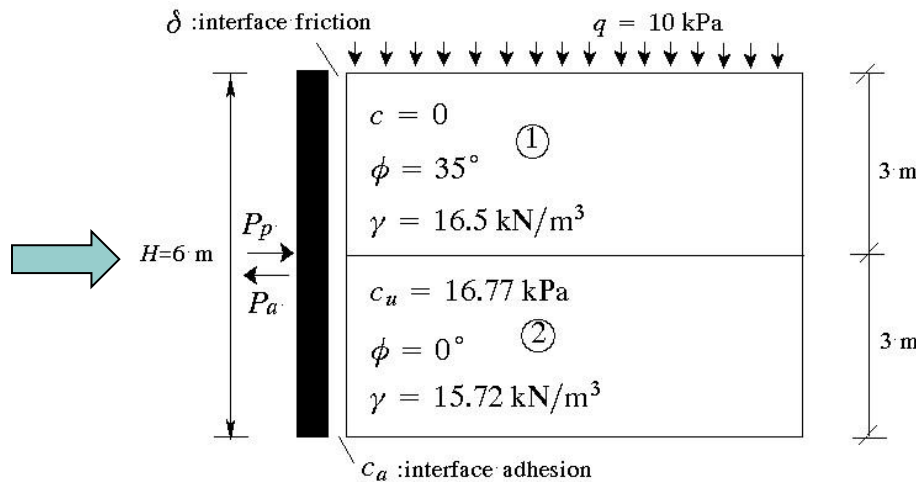
# Smooth case - Passive wall

- FLAC solution
- Textbook solution – Rankine
- Upper and Lower bound solutions



# Textbook solution of the problem

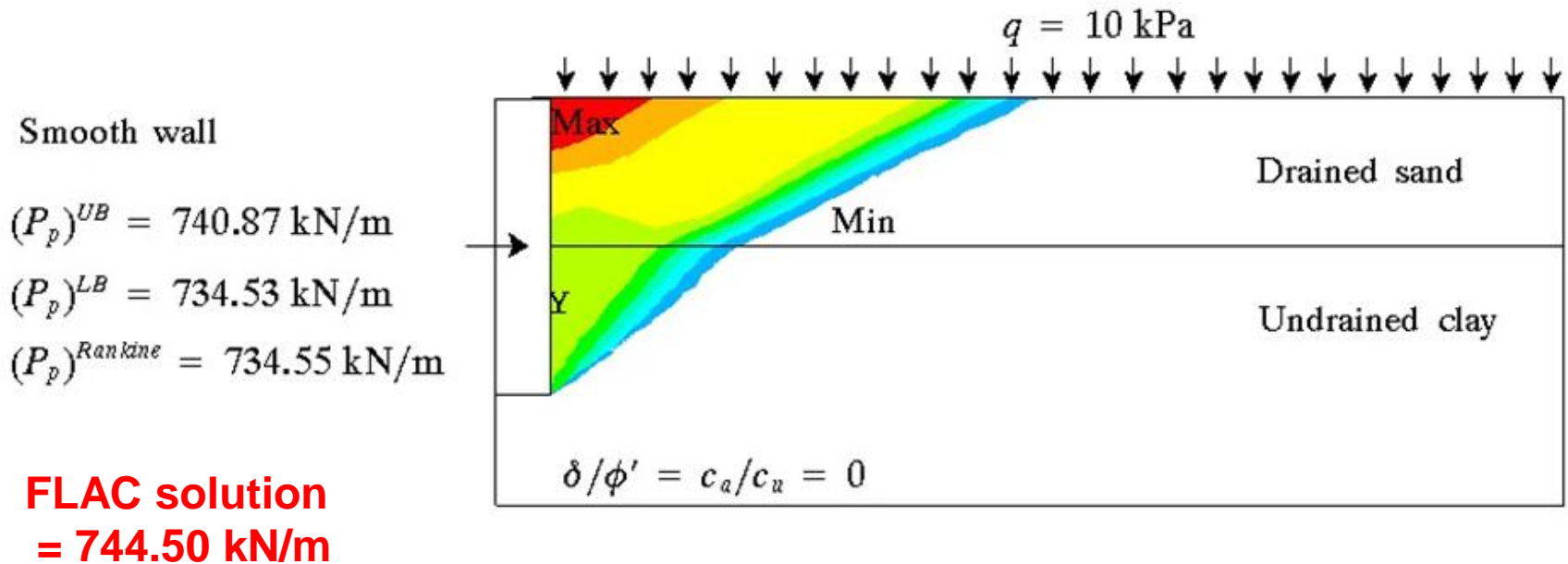
Passive wall – Smooth wall case – Rankine's solution

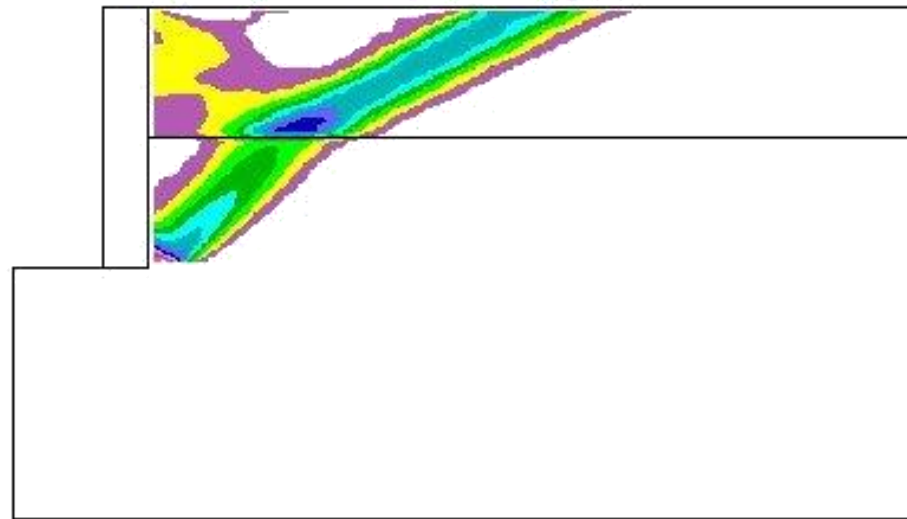
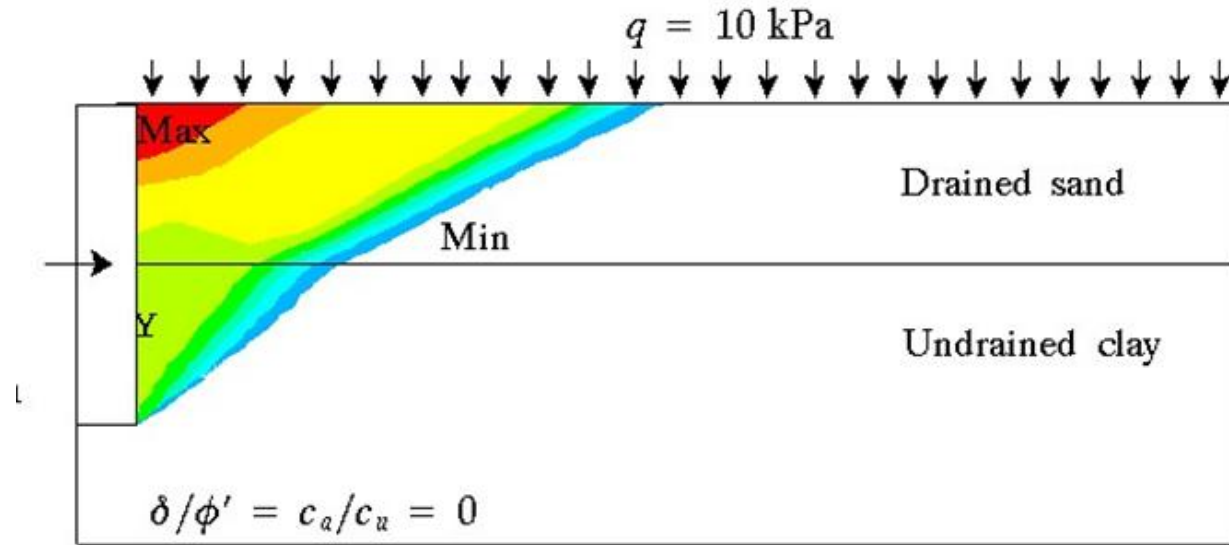


Rankine: Total horizontal passive thrust = 734.55 kN/m  
 FLAC solution = 744.50 kN/m

# Upper and lower bound solutions of the problem

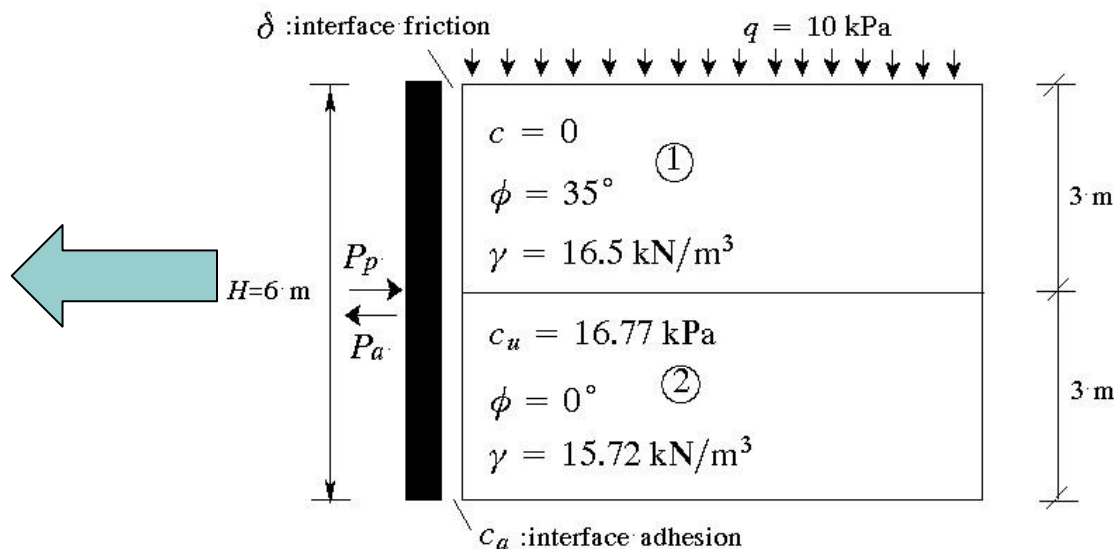
Passive wall – smooth wall case





# Rough case - Active wall

- FLAC solution
- Textbook solution – Coulomb
- Upper and Lower bound solutions



# Upper and lower bound solutions of the problem

Active wall – rough wall case

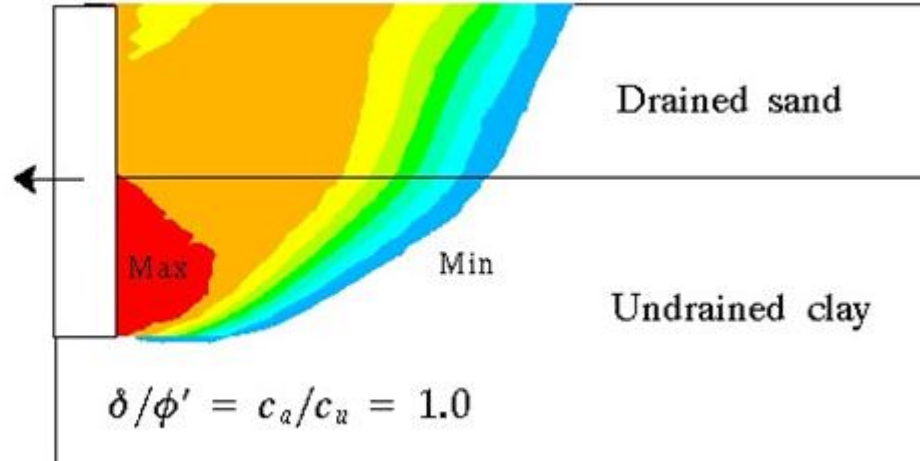
Rough wall

$$(P_a)^{UB} = 124.58 \text{ kN/m}$$

$$(P_a)^{LB} = 133.07 \text{ kN/m}$$

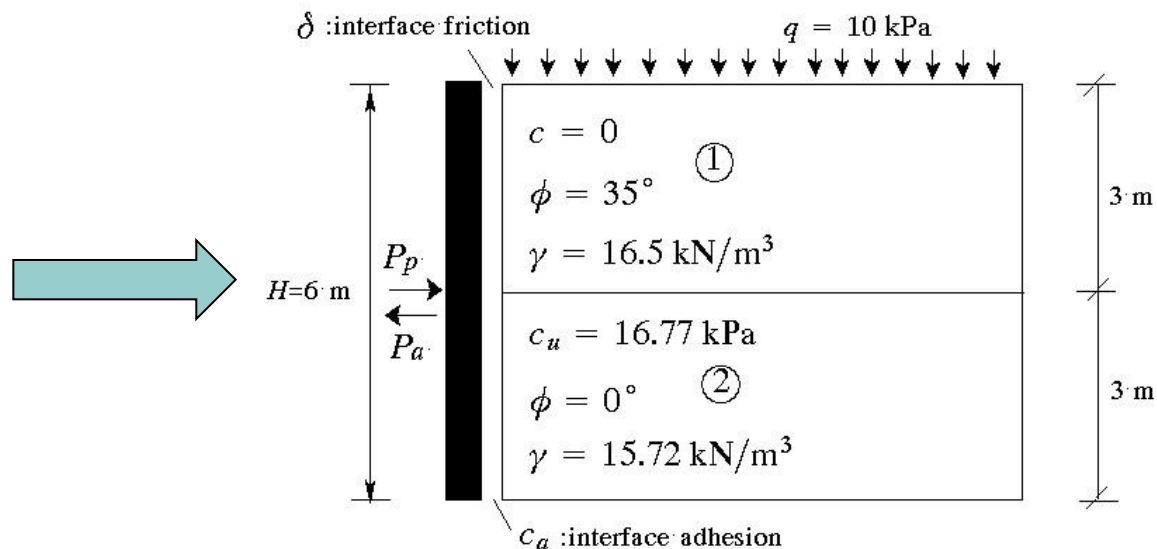
$$\text{Coulomb} = 128.80 \text{ kN/m}$$

**FLAC solution**  
**= 127.60 kN/m**



# Rough case - Passive wall

- FLAC solution
- Textbook solution – Coulomb
- Upper and Lower bound solutions





# Upper and lower bound solutions of the problem

Passive wall – rough wall case

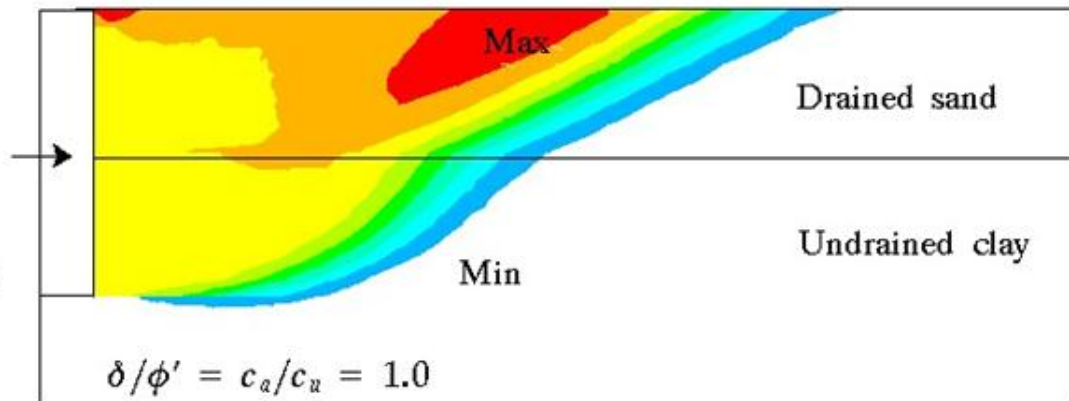
Rough wall

$$(P_p)^{UB} = 844.24 \text{ kN/m}$$

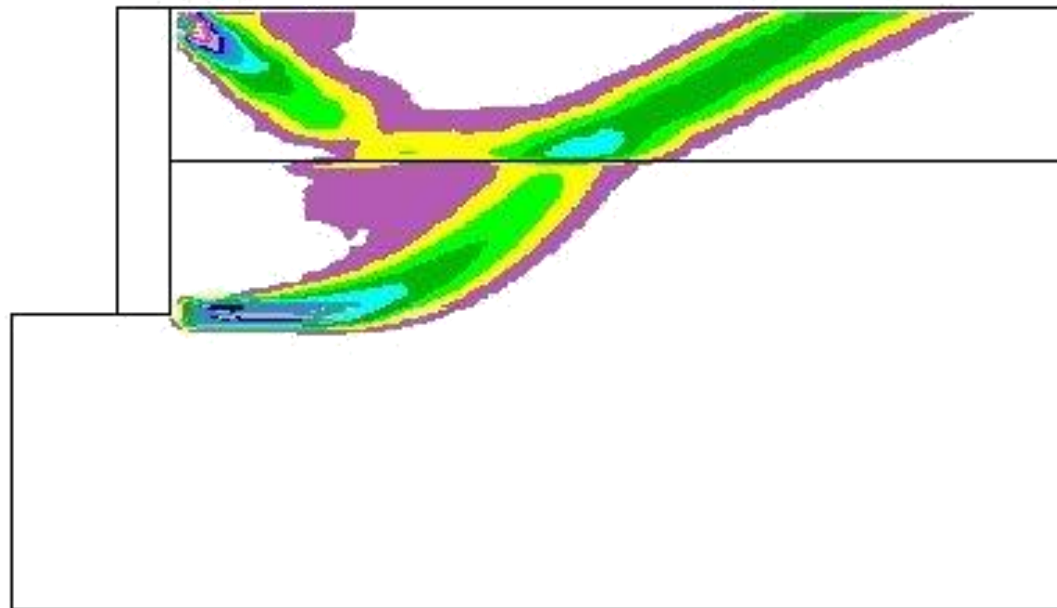
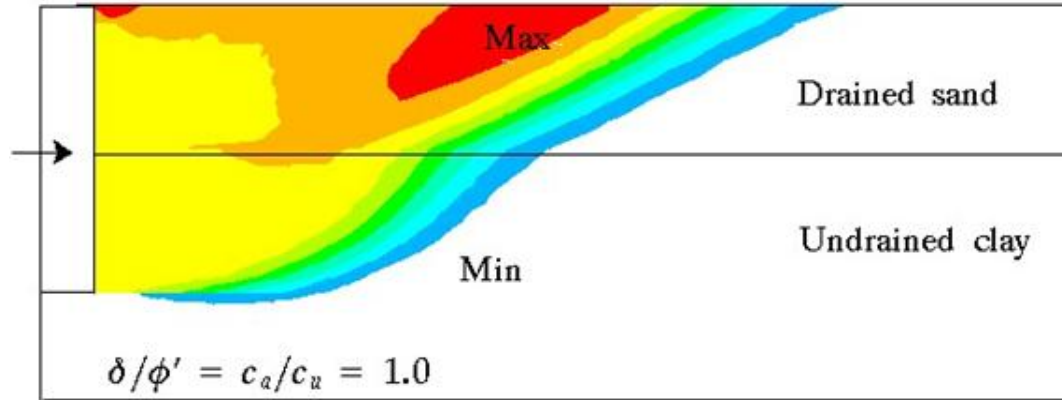
$$(P_p)^{LB} = 826.95 \text{ kN/m}$$

$$\text{Log-Spiral} = 1010.70 \text{ kN/m}$$

$$\text{Coulomb} = ???$$



**FLAC solution**  
**= 837.20 kN/m**



# Results Summary

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Table 3. Comparison of results for active force (kN/m).

Active walls	Rankine / Coulomb	LB	UB	<i>FLAC</i>
Smooth wall	176.18	173.21	166.35	167.20
Rough wall	128.80	133.07	124.58	127.60

Table 4. Comparison of results for passive resistance (kN/m).

Passive walls	Rankine / Log-Spiral	LB	UB	<i>FLAC</i>
Smooth wall	734.55	734.53	740.87	744.50
Rough wall	1010.7	826.95	844.24	837.20

# Summary

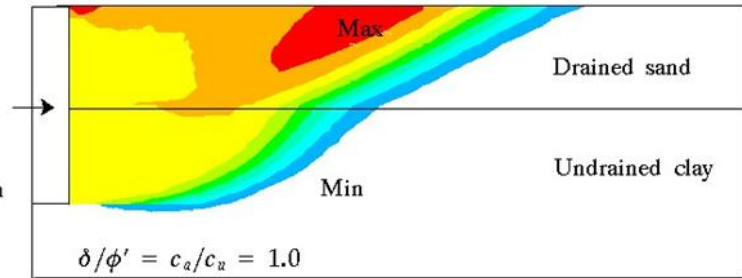
Rough wall

$$(P_p)^{UB} = 844.24 \text{ kN/m}$$

$$(P_p)^{LB} = 826.95 \text{ kN/m}$$

$$\text{Log-Spiral} = 1010.70 \text{ kN/m}$$

$$\text{Coulomb} = ???$$



- **FLAC results favorably compared with upper and lower bound solutions in all cases.**
- **Classical earth pressure theories favorably compared with FLAC and upper and lower bound solutions **only in smooth wall cases (active and passive) and rough active wall case.****
- **For the rough passive wall case, the log-spiral failure surface Shields & Tolunay's (1973) theory is not particularly accurate for the layered problem. It's on the unsafe side with some 20% overestimation ~ needless to mention Coulomb's solution with linear slip assumption.**

# Future Work

- Pressure distribution behind the wall.
- Velocity jump and change of velocity direction across layered media.
- Shear stresses across the layered media for the passive + rough wall case

Rough wall

$$(P_p)^{UB} = 844.24 \text{ kN/m}$$

$$(P_p)^{LB} = 826.95 \text{ kN/m}$$

$$\text{Log-Spiral} = 1010.70 \text{ kN/m}$$

$$\text{Coulomb} = ???$$

