

Problem 1.1

Data:

$$\delta = 7000 \text{ N/m}^3, \quad \rho = ?, \quad V = ?, \quad S = ?$$

$$T = 15^\circ \text{C}$$

Sol:

$$a) \quad \delta = \rho g \Rightarrow \rho = \frac{\delta}{g} = \frac{7000}{9.81} = 713.55 \text{ kg/m}^3$$

$$b) \quad V = \frac{1}{\rho} = \frac{1}{713.55} = 1.4 \times 10^{-3} \text{ m}^3/\text{kg}$$

$$c) \quad S = \frac{\delta_{\text{gasoline}}}{\delta_{\text{water}}} = \frac{7000}{9.798 \times 10^3} = 0.7144$$

Prob. 1.2

Data:

$$\delta_{\text{gas}} = 16 \text{ N/m}^3, \quad \rho = ?, \quad V = ?, \quad S = ?$$

$$\delta_{\text{air}} = 12 \text{ N/m}^3$$

Sol:

$$a) \quad \delta = \rho g \Rightarrow \rho = \frac{\delta}{g} = \frac{16}{9.81} = 1.63 \text{ kg/m}^3$$

$$b) \quad V = \frac{1}{\rho} = \frac{1}{1.63} = 0.613 \text{ m}^3/\text{kg}$$

$$c) \quad S = \frac{\delta_{\text{gas}}}{\delta_{\text{air}}} = \frac{16}{12} = 1.33$$

Prob. 1.3

Data:

$$S_{fluid} = 1.26$$

$$\rho = ?$$

$$\gamma = ?$$

Sol:

$$S = \frac{\rho_{fluid}}{\rho_{water}} \Rightarrow \rho_{fluid} = 1.26 \times 1000 = 1260 \text{ kg/m}^3$$

$$\gamma = \rho g = 1260 \times 9.81 = 12360.6 \text{ N/m}^3$$

Prob 1.4

Data:

$$\gamma = 8 \text{ kN/m}^3 = 8 \times 10^3 \text{ N/m}^3$$

$$\rho = ?$$

Sol:

$$\gamma = \rho g$$

$$\rho = \frac{\gamma}{g} = \frac{8 \times 10^3}{9.81} = 815.49 \text{ kg/m}^3$$

Prob 1.5

Data:

$$\gamma = 0.72 \text{ m}^3/\text{kg}$$

$$\gamma = ? \text{ in N/m}^3$$

Sol:

$$\gamma = \rho g$$

$$= \frac{1}{\gamma} g = \frac{1}{0.72} \times 9.81 = 13.625 \text{ N/m}^3$$

Prob 1.7

Data:

$$P_2 = 100 \text{ MN/m}^2$$

$$T = 20^\circ\text{C}$$

$$P_1 = 100 \text{ kN/m}^2 = 0.1 \text{ MN/m}^2$$

$$\% \text{ dec. in specific volume} = \frac{V_1 - V_2}{V_1} \times 100 = ?$$

Sol:

$$(E_v)_{\text{avg}} = \frac{\Delta P}{\Delta V/V}$$

$$\frac{V_1 - V_2}{V_1} \times 100 = \frac{P_2 - P_1}{(E_v)_{\text{avg}}} \times 100$$

$$= \frac{100 - 0.1}{2430} \times 100 = 4.11\%$$

From table 1.1

$$P_1 = 0.1 \text{ MN/m}^2$$

$$E_v = 2130 \text{ MN/m}^2$$

$$P_2 = 100 \text{ MN/m}^2$$

$$E_v = 2730 \text{ MN/m}^2$$

$$(E_v)_{\text{avg}} = \frac{2730 + 2130}{2} = 2430 \text{ MN/m}^2$$

Prob 1.8

Data:

$$(E_v)_{\text{avg}} = 2.34 \times 10^9 \text{ N/m}^2$$

$$\delta_1 = 10.05 \text{ kN/m}^2 \quad P_1 = 101.31 \text{ kN/m}^2$$

a) $V_1 - V_2$

b) $V_2 = ?$

c) $\delta_2 = ?$

8 km

$$P_2 = 81.8 \text{ MPa}$$

Sol:

$$a) (\bar{E}_v)_{avg} = \frac{\Delta P}{\Delta V/V} = \frac{P_2 - P_1}{(V_1 - V_2)/V_1}$$

$$V_1 - V_2 = \frac{(P_2 - P_1) V_1}{(\bar{E}_v)_{avg}}$$
$$= \frac{(81.8 \times 10^6 - 101300) \times 9.76 \times 10^{-4}}{2.34 \times 10^5}$$

$$\delta = \rho g$$
$$\delta_1 = \frac{1}{V_1} \rho g$$
$$V_1 = \frac{9.81}{10.05 \times 10^3}$$
$$V_1 = 9.76 \times 10^{-4} \text{ m}^3/\text{kg}$$

$$V_1 - V_2 = 3.407 \times 10^{-5} \text{ m}^3/\text{kg}$$

$$b) V_1 - V_2 = 3.407 \times 10^{-5} \text{ m}^3/\text{kg}$$

$$9.76 \times 10^{-4} - V_2 = 3.407 \times 10^{-5}$$

$$V_2 = 9.41 \times 10^{-4} \text{ m}^3/\text{kg}$$

$$c) \delta_2 = \frac{1}{V_2} \rho g$$

$$= \frac{9.81}{9.41 \times 10^{-4}} = 10425.07 \text{ N/m}^3$$

Prob. 1.9

Data:

$$a) \% \text{ change in } V \text{ in } 1.8 = \frac{V_1 - V_2}{V_1} \times 100 = ?$$

$$b) \% \text{ change in } \delta \text{ in } 1.8 = \frac{\delta_1 - \delta_2}{\delta_1} \times 100 = ?$$

Sol:

$$a) \frac{V_1 - V_2}{V_1} \times 100 = \frac{3.407 \times 10^{-5}}{9.76 \times 10^{-4}} \times 100 = 3.49 \%$$

$$b) \frac{\delta_2 - \delta_1}{\delta_1} \times 100 = \frac{10425.07 - 10050}{10050} \times 100 = 3.73 \%$$

Prob. 1.10

Data:

$$E_v = ? \quad \text{in MN/m}^2$$

$$T = 50^\circ\text{C}$$

$$P = 30 \text{ MN/m}^2$$

Sol:

By using table 1.1

$$\text{Bulk modulus} = E_v = 2410 \text{ MN/m}^2 \text{ at } 50^\circ\text{C}$$

Prob. 1.11

Data:

$$P = ?$$

For reduction of vol. of H_2O 2%.

we should put

$$\frac{V_1 - V_2}{V_1} \times 100 = 2$$

$$\frac{V_1 - V_2}{V_1} = 2/100$$

$$\text{So } E_v = \frac{P_2 - P_1}{\frac{V_1 - V_2}{V_1}}$$

$$\frac{V_1 - V_2}{V_1} = \frac{P_2 - P_1}{E_v}$$

$$P_2 - P_1 = \Delta P = \frac{V_1 - V_2}{V_1} \times E_v$$

$$= \frac{2}{100} \times (2.18 \times 10^6 \text{ N/m}^2)$$

$$= 43600 \text{ N/m}^2$$

Prob 1.27

Data:

$$1 \text{ cP} = 10^{-3} \text{ Ns/m}^2$$

$$\mu = 23 \text{ cP} = 23 \times 10^{-3} \text{ Ns/m}^2$$

$$\gamma = 8.4 \text{ kN/m}^3 = 8.4 \times 10^3 \text{ N/m}^3$$

$$\nu = ?$$

Sol:

$$\nu = \frac{\mu}{\rho}$$
$$= \frac{23 \times 10^{-3}}{856.26}$$

$$\gamma = \rho g$$

$$\rho = \frac{\gamma}{g} = \frac{8.4 \times 10^3}{9.81} = 856.26 \text{ kg/m}^3$$

$$\nu = 2.6 \times 10^{-5} \text{ m}^2/\text{s}$$

Prob 1.28

Data:

a) Water: $\frac{\mu_{20^\circ\text{C}}}{\mu_{40^\circ\text{C}}} = \frac{1.002 \times 10^{-3}}{0.315 \times 10^{-3}} = 3.180$

b)

crude oil $T = 150^\circ\text{C}$
gasoline $\frac{\mu_{0.925}}{\mu_{0.680}} = \frac{1.0 \times 10^{-1} \text{ Ns/m}^2}{3.3 \times 10^{-4}} = 300$

c)

change μ of SAE 30 western = $\frac{0.04 - 3}{0.03 - 1.5}$

change μ of SAE 30 eastern = $\frac{0.03 - 1.5}{0.04 - 3} = 2.01$

Prob. 1.29:

Data:

$$T = 15^\circ\text{C}$$

$$\nu_{\text{gasoline}} = ?$$

$$S = 0.680$$

Sol:

$$\text{From figure 1.3: } \nu_{\text{gasoline}} = 4.8 \times 10^{-7} \text{ m}^2/\text{s}$$

Prob 1.30:

$$\nu_{\text{water at } 4^\circ\text{C}} = 1.57 \times 10^{-6} \text{ m}^2/\text{s}$$

Using Relation

$$\nu_{\text{fuel}} = 3 \nu_{\text{water}}$$

$$= 3 \times 1.57 \times 10^{-6} = 4.71 \times 10^{-6} \text{ m}^2/\text{s}$$

This Kinematic viscosity is at temp. = 198°C

Prob. 1.32:

Compare $\frac{\mu_{\text{air at } 20^\circ\text{C}}}{\rho_{\text{water at } 20^\circ\text{C}}}$ with $\frac{\nu_{\text{air at } 20^\circ\text{C}}}{\nu_{\text{water at } 20^\circ\text{C}}}$

Sol:

$$\frac{1.81 \times 10^{-5}}{1.002 \times 10^{-3}} = 0.01806 \quad \frac{1.5 \times 10^{-5}}{1.003 \times 10^{-6}} = 14.95$$

$$\text{Diff.} = 14.95 - 0.01806 \\ = 14.93$$

Prob. 1.33

Data:

$$A = 30 \text{ cm} \times 50 \text{ cm} = 1500 \text{ cm}^2 = 0.15 \text{ m}^2$$

$$\mu = 0.8 \text{ N s/m}^2$$

$$u = 2 \text{ m s}^{-1}$$

$$y = 0.4 \text{ mm} = 0.4 \times 10^{-3} \text{ m}$$

$$F = ?$$

Sol:

$$F = \frac{\mu u A}{y}$$

$$F = \frac{2 \times 0.8 \times 0.15}{0.4 \times 10^{-3}} = 600 \text{ N}$$

Prob 1.34

Data:

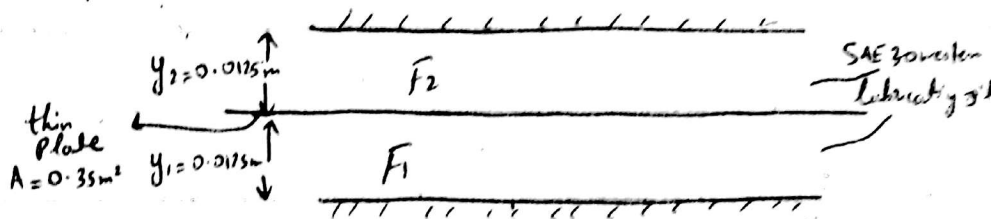
$$y = 25 \text{ mm} = 0.025 \text{ m}$$

$$T = 25^\circ \text{C}$$

a) $F = ?$

$$A = 0.35 \text{ m}^2$$

$$u = 0.1 \text{ m/s}$$



Sol:

$$F = F_1 + F_2$$

$$F_1 = \frac{\mu u A}{y} = \frac{(0.3)(0.1)(0.35)}{0.0125}$$

From fig 1.2 Pg 11

$$F = 0.84 + 0.84$$

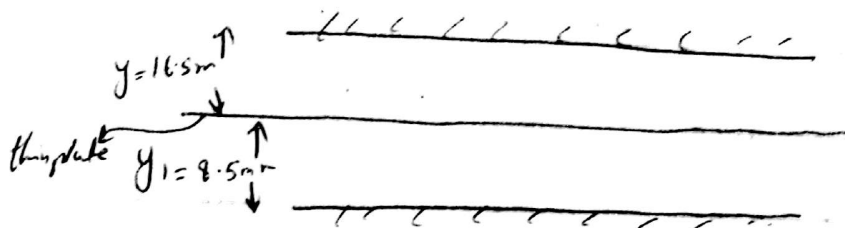
$$F = 1.68 \text{ N}$$

$$= 0.84$$

$$F_2 = 0.84$$

b)

$y = 25 \text{ mm}$
 $F = ?$



$$F_1 = \frac{(0.3)(0.1)(0.35)}{8.5 \times 10^{-3}}$$

$$F_1 = 1.235 \text{ N}$$

$$F_2 = \frac{(0.3)(0.1)(0.35)}{16.5 \times 10^{-3}}$$

$$F_2 = 0.636 \text{ N}$$

$$F = 1.235 + 0.636$$

$$F = 1.87 \text{ N}$$

Prob. 1.42

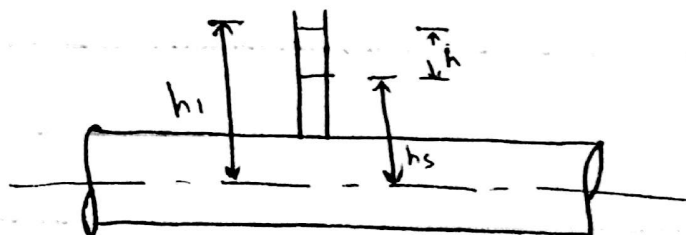
Data: Distilled water

$$T = 10^\circ \text{C}$$

$$d = 8 \text{ mm} = 8 \times 10^{-3} \text{ m}$$

$$h_1 = 25 \text{ mm} = 25 \times 10^{-3} \text{ m}$$

$$h_s = ?$$



Sol:

$$h_s = h_1 - h$$

$$h_s = 25 \times 10^{-3} - 3.78 \times 10^{-3}$$

$$h_s = 21.22 \times 10^{-3} \text{ m}$$

$$h_s = 21.22 \text{ mm of water}$$

$$h = \frac{4 \sigma \cos \theta}{\rho g d}$$

$$\rho = 999.7 \times 9.8$$

$$h = \frac{4 (0.0742) \cos 0}{9.807 \times 10^3 \times 8 \times 10^{-3}}$$

$$\rho = 9807.05$$

$$9.807 \times 10^3 \times 8 \times 10^{-3}$$

$$h = 3.78 \times 10^{-3} \text{ m}$$

Prob. 1.43

Data: Tap water

$$T = 20^\circ\text{C}$$

$$d = 8\text{ mm} = 8 \times 10^{-3}\text{ m}$$

$$h_i = 11.25\text{ mm} = 11.25 \times 10^{-3}\text{ m}$$

$$h_s = ?$$

Sol:

$$h_s = h_i - h$$
$$= 11.25 - 1.45$$

$$h = 1.45\text{ mm}$$

(capillarity rise)

$$h_s = 9.8\text{ mm}$$

Prob. 1.44

Data:

Capillary Rise = ?

Fluid = Water $d = 5\text{ mm}$

$$T = 20^\circ\text{C}$$

Sol:

$$h = \frac{4\sigma \cos\theta}{\rho g d} = \frac{4\sigma \cos\theta}{\rho g d} = \frac{4(0.0728)\cos 0^\circ}{998.2 \times 9.81 \times 5 \times 10^{-3}}$$

$$h = 5.947 \times 10^{-3}\text{ m}$$

$$h = 5.95\text{ mm}$$

Prob. 1.45

Data

Capillary depression = ?

$$\theta = 140^\circ$$

$$d = 2.5 \text{ mm}$$

$$\sigma = 0.4841 \text{ N/m}$$

$$\rho_{\text{Hg}} = 13550 \text{ kg/m}^3$$

Fluid = Mercury

$$T = 20^\circ$$

Sol:

$$h = \frac{4\sigma \cos\theta}{(\rho g)d} = \frac{4(0.4841) \cos 140^\circ}{13550 \times 9.81 \times 2.5 \times 10^{-3}}$$

$$h = -4.27 \times 10^{-3} \text{ m}$$

$$h = 4.27 \text{ mm fall}$$

Prob. 12.6

Data:

Type = Rotational

$$h = 25 \text{ cm} = 0.25 \text{ m}$$

Outer diameter of inner cylinder = $d_1 = 9.9 \text{ cm} = 0.099 \text{ m} \Rightarrow r_1 = 0.0495$

Inner diameter of outer cylinder = $d_2 = 10.1 \text{ cm} = 0.101 \text{ m} \Rightarrow r_2 = 0.0505$

$T = 7 \text{ Nm}$ on outer cylinder

$$N = \frac{1 \text{ rev}}{3.5 \text{ s}} = \frac{1 \text{ rev}}{\frac{3.5}{60} \text{ min}} = 17.14 \text{ rev/min}$$

$\mu = ?$

Sol:

$$\mu = \frac{T}{K \Delta r}$$

$$\mu = \frac{7}{0.0212 \times 17.14} = 19.26 \text{ Ns/m}^2$$

$$K \Delta r = \frac{\pi^2 r_2^3 h}{15 \Delta r}$$

$$K \Delta r = \frac{\pi^2 (0.0505)^3 (0.25)}{15 (0.0505 - 0.0495)}$$

$$K \Delta r = 0.0212 \text{ m}^3$$

Prob. 12.7

Data:

Type = Tube type

$$D = 1.07 \text{ mm} = 1.07 \times 10^{-3} \text{ m}$$

$$L = 7.75 \text{ cm} = 7.75 \times 10^{-2} \text{ m}$$

$v = ?$

$$V_L = 50 \text{ cm}^3 = 50 \times 10^{-6} \text{ m}^3$$

$$t = 126.4 \text{ s}$$

Distance from h_2 surface to the tube outlet changes from 24 → 22.8 cm

Mean

$$h_1 + L = 24 \text{ cm} \quad \text{--- (1)}$$

$$h_1 + L = 0.24$$

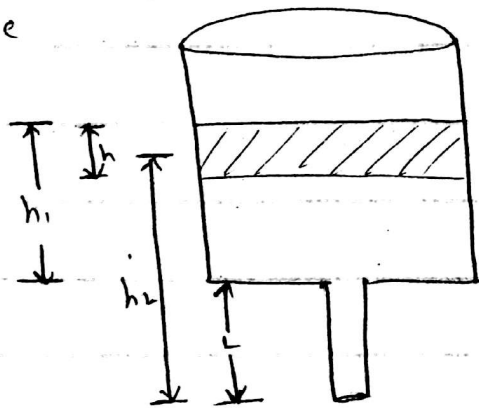
$$h_1 = 0.24 - 7.75 \times 10^{-2}$$

$$\boxed{h_1 = 0.1625 \text{ m}}$$

$$h_L = h_1 + L - \frac{h}{2}$$

$$h_L = 0.1625 + 7.75 \times 10^{-2} - \frac{0.012}{2}$$

$$\boxed{h_L = 0.234 \text{ m}}$$



and

$$h_L - \frac{h}{2} = 22.8 \text{ cm} \quad \text{--- (2)}$$

$$h_L - \frac{h}{2} = 0.228$$

$$h_1 + L - \frac{h}{2} - \frac{h}{2} = 0.228$$

$$h_1 + L - h = 0.228$$

$$0.1625 + 7.75 \times 10^{-2} - 0.228 = h$$

$$\boxed{h = 0.012 \text{ m}}$$

Sol:

$$v = K_t g t$$

$$v = 1.94 \times 10^{-9} \times 9.81 \times 126.4$$

$$v = 2.4 \times 10^{-6} \text{ m}^2/\text{s}$$

$$K_t = \frac{\pi D^4 h_L}{128 L V_L}$$

$$= \frac{\pi (1.07 \times 10^{-3})^4 (0.234)}{128 (7.75 \times 10^{-2}) (50 \times 10^{-6})}$$

$$K_t = 1.94 \times 10^{-9} \text{ m}$$

Prob. 12.8

Data:

Water Type = Tube type

$$V_L = 50 \text{ cm}^3$$

$$T_1 = 25^\circ\text{C}$$

$$t_1 = 50.5 \text{ s}$$

$$\text{Oil } V_L = 50 \text{ cm}^3$$

$$T_2 = 15^\circ\text{C}$$

$$t_2 = 800 \text{ s}$$

$$S = 0.86$$

$$\mu_2 = ?$$

Sol:

$$\mu_1 = K_t \delta_1 t_1$$

$$K_t = \frac{\mu_1}{\delta_1 t_1}$$

$$= \frac{0.890 \times 10^{-3}}{(997 \times 9.81)(50.5)}$$

$$K_t = 1.8 \times 10^{-9} \text{ m}$$

$$\mu_2 = K_t \delta_2 t_2$$

$$\mu_2 = 1.8 \times 10^{-9} (8411.29)(800)$$

$$\boxed{\mu_2 = 0.012 \text{ Ns/m}^2}$$

$$S = \frac{\rho_{\text{fluid}}}{\rho_{\text{water}}}$$

$$\rho_{\text{fluid}} = 0.86 \times 997$$

$$= 857.42 \text{ kg/m}^3$$

$$\delta_2 = \rho_{\text{fluid}} \times g$$

$$= 857.42 \times 9.81$$

$$\delta_2 = 8411.29 \text{ N/m}^3$$

12.9

Data:

$$\rho = 880 \text{ kg/m}^3 \quad D = 2 \text{ mm} = 2 \times 10^{-3} \text{ m} \Rightarrow \delta = 10^{-3} \text{ m}$$

$$L = 4.5 \text{ m} \quad h_L = 50 \text{ cm} = 0.5 \text{ m} \quad \frac{V}{t} = \frac{30 \text{ cm}^3}{\text{min}} = \frac{30}{60 \times 10^6} \frac{\text{m}^3}{\text{s}} = 0.5 \times 10^{-6} \frac{\text{m}^3}{\text{s}}$$

$\mu = ?$ $\nu = ?$
 in poise in Stokes

Sol:

$$V = \frac{h_L \delta D^2}{32 \mu L} \quad \therefore \delta = \rho g = 880 \times 9.81 = 8632.8 \text{ N/m}^3$$

$$AV = \frac{V}{t}$$

$$a) \mu = \frac{(0.5)(8632.8)(2 \times 10^{-3})^2}{(32)(0.1591)(4.5)}$$

$$V = \frac{0.5 \times 10^{-6}}{\pi (10^{-3})^2}$$

$$\mu = 7.53 \times 10^{-4} \text{ N s/m}^2$$

$$\therefore V = 0.1591 \text{ m/s}$$

$$\mu = 7.53 \times 10^{-4} \times 10 \text{ poise}$$

$$\mu = 7.53 \times 10^{-3} \text{ poise}$$

$$\therefore 10 \text{ poise} = 1 \text{ N s/m}^2$$

$$b) \nu = \frac{\mu}{\rho} = \frac{7.53 \times 10^{-4}}{880}$$

$$= 8.56 \times 10^{-7} \text{ m}^2/\text{s}$$

$$= 8.56 \times 10^{-3} \text{ Stokes} \quad \therefore 10^4 \text{ Stokes} = 1 \text{ m}^2/\text{s}$$

Ca

1

12.10

Data:

$T_1 = 10^\circ\text{C}$ liquid = Water

Type = type type

$t_1 = 100\text{s}$

$T_2 = 38^\circ\text{C}$

$t_2 = ?$

Sol:

$$\mu_1 = K_t \delta_1 t_1$$

$$\mu_2 = K_t \delta_2 t_2$$

$$K_t = \frac{\mu_1}{\delta_1 t_1}$$

$$t_2 = \frac{\mu_2}{K_t \delta_2}$$

$$= \frac{1.307 \times 10^{-3}}{9804 \times 100}$$

$$= \frac{0.622 \times 10^{-3}}{1.33 \times 10^{-9} \times 9736.8}$$

$$K_t = 1.33 \times 10^{-9} \text{ m}$$

$$t_2 = 52.66 \text{ s}$$

Calculations

δ at $10^\circ\text{C} = 9.804 \text{ KN/m}^3$ and δ at $38^\circ\text{C} =$

μ_1 at $10^\circ\text{C} = 1.307 \times 10^{-3} \text{ N s/m}^2$ and μ_2 at $38^\circ\text{C} =$

| $T^\circ\text{C}$ | $\delta \text{ (KN/m}^3\text{)}$ | $\mu \text{ (}\times 10^{-3}\text{) N s/m}^2$ |
|-------------------|----------------------------------|---|
| 30 | 9.764 | 0.798 |
| 40 | 9.730 | 0.653 |

| | | |
|--|--|--|
| Difference = 10°C | 0.034 | 0.145 |
| 1°C | 3.4×10^{-3} | 0.0145 |
| $1 \times 8^\circ\text{C}$ | 0.0272 | 0.116 |
| At $38^\circ\text{C} = 30^\circ + 8^\circ =$ | 9.764 | 0.798 |
| | $- 0.0272$ | $- 0.116$ |
| | <u>9.7368 KN/m^3</u> | <u>$0.682 \times 10^{-3} \text{ N s/m}^2$</u> |