

**FLUID MECHANICS-II**  
**(6<sup>th</sup> Term B.Sc. Civil Engineering)**  
**(Session-2014)**  
**Teacher Incharge: Prof. Dr. Habib-ur-Rehman**

**Assignment No. 4**  
**(Centrifugal Pump)**

**Part (A):**

Go through Solved Examples 14.1, 14.2, 14.5 of Text Book, "Solving Problems in Fluid Mechanics" Vol-2, By J. F. Douglas.

**Part (B):**

Go through Solved Example 14.1 of Text Book "Fluid Mechanics with Practical Applications by Daugherty (8<sup>th</sup> or S.I edition).

**Part (C):**

Solve the following numerical problems.

- Q. No.1.** The diameter of an impeller of a pump is 1.20 m and its peripheral speed is 9 m/s. Water enters radially and is discharges from the impeller with a velocity whose radial component is 1.50 m/s. The vanes are curved backwards at exit and make an angle of 30° with the periphery. If the pump discharges 3.40 m<sup>3</sup>/min, what will be the turning moment on the shaft. (217.6 N-m)
- Q. No.2.** A pump delivers 1.27 m<sup>3</sup> of water per minute at 1200 rev/min. The impeller diameter is 350 mm and breadth at outlet 12.7 mm. The pressure difference between inlet and outlet flanges is 272 kN/m<sup>2</sup>. Taking manometric efficiency as 63 %, calculate the impeller exit blade angle. (32.39°)
- Q. No.3.** If the static suction and delivery lifts of a pump are 5 m and 6 m respectively. Dia. of suction pipe is 10 cm and of delivery 8 cm. If the pumping capacity of a pump is 0.08 cumecs of water. Calculate (a) manometric suction head, (b) manometric delivery head (c) total manometric head, (d) power developed by the pump. Use  $f = 0.031$  both for suction and delivery pipes. (19.3 m, 43.636 m, 62.94 m, 49.395 KW)
- Q. No.4.** Calculate the maximum suction lift for a centrifugal pump if it discharges 50 lit/s. Dia of suction pipe is 15 cm. Barometric pressure is 100 kN/m<sup>2</sup> abs. and vapor pressure for water is 2.34 kN/m<sup>2</sup> abs. Frictional losses in the pipe are  $2 V^2/2g$ . (8.731 m)

CP

Q.1

Datu:

$$D = 1.2 \text{ m}$$

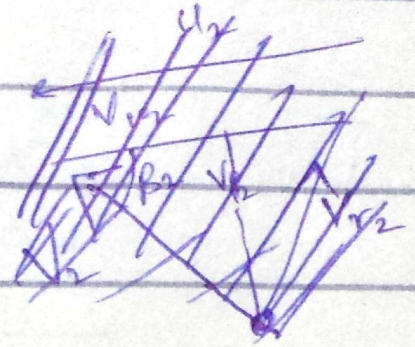
$$U = 9 \text{ m/s}$$

$$V_{f2} = 1.5 \text{ m/s}$$

$$\theta_2 = 30^\circ$$

$$Q = 3.4 \text{ m}^3/\text{min} = 56.667 \times 10^{-3} \text{ m}^3/\text{s}$$

$$T = ?$$



Sol:

Applying IME in radial direction

$$(\Sigma F)_x = \rho Q (V_{w2} - V_{w1})$$

$$-F = \rho Q (-V_{w2} - 0)$$

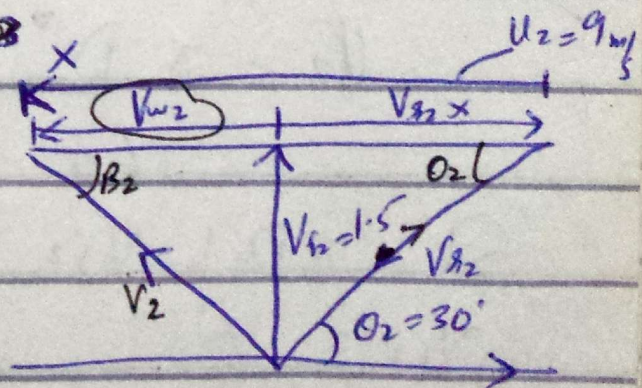
$$F = \rho Q V_{w2}$$

~~Q = \dots~~

~~Q = \dots~~

$$\tan 30^\circ = \frac{1.5}{V_{f2x}}$$

$$V_{f2x} = 2.6 \text{ m/s}$$





# SEISMIC GROUP VET LHR

$$V_{w2} = U_2 - V_{r2} \times$$

$$V_{w2} = 9 - 2.6 = 6.4 \text{ m/s}$$

$$F = \rho \cdot V_{w2}$$

$$= 1000 \times 56.67 \times 10^{-3} \times 6.4$$

$$F = 362.68 \text{ N}$$

$$T = F \times r$$

$$= 362.68 \times 0.6 = 217.6 \text{ Nm}$$

Q=2

~~Q=2~~  $V = 1.27 \text{ m}^3$

$$t = 1 \text{ min}$$

$$Q = 21.17 \times 10^{-3} \text{ m}^3/\text{s}$$

$$N = 1200 \text{ rev/min}$$

$$D = 350 \text{ mm}$$

$$b_2 = 12.7 \text{ mm}$$

$$P_1 - P_2 = 272 \text{ kN/m}^2$$

$$\eta_m = 63\%$$

$$\theta_2 = ?$$

Sol:

$$U_2 = \frac{\pi D^2 N}{60} = \frac{\pi \times 0.35^2 \times 1200}{60} = 2.2 \text{ m/s}$$

$$Q_2 = \pi D_2 b_2 V_{f2}$$

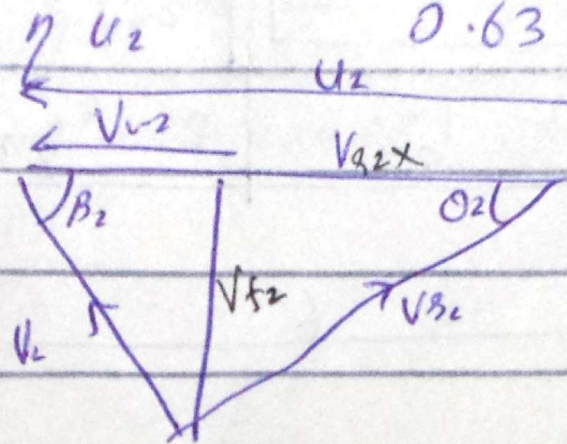
$$V_{f2} = \frac{Q}{\pi D_2 b_2} = \frac{21.17 \times 10^{-3}}{\pi \times 0.33 \times 0.0127} = 1.52$$



$$H = \frac{P_2}{\rho} = \frac{272 \times 10^3}{9810} = 27.73 \text{ m}$$

$$\eta = \frac{gH}{V_{w2} U_2}$$

$$V_{w2} = \frac{gH}{\eta U_2} = \frac{9.81 \times 27.73}{0.63 \times 22} = 19.63 \text{ m/s}$$



$$U_2 = V_{w2} + V_{g2x}$$

$$V_{g2x} = U_2 - V_{w2}$$

$$= 22 - 19.63 = 2.37 \text{ m/s}$$

$$\theta = \tan^{-1} \left( \frac{V_{f2}}{U_2 - V_{w2}} \right)$$

$$= \tan^{-1} \left( \frac{1.53}{2.37} \right) = 32.81^\circ$$



$$Q = 3$$

Data:

$$H_s = 5 \text{ m}$$

$$H_d = 6 \text{ m}$$

$$D_s = 10 \text{ cm} = 0.1 \text{ m}$$

$$D_d = 8 \text{ cm} = 0.08 \text{ m}$$

$$Q = \text{pumping capacity} = 0.03 \text{ m}^3/\text{s}$$

a)  $H_{ms} = ?$

b)  $H_{md} = ?$       c)  $H_m = ?$

~~DA~~ Power developed = ?

$$f = 0.031 \quad (\text{Both for suction and delivery})$$

Sol:

$$a) H_{ms} = H_s + H_{fs} + \frac{V_s^2}{2g}$$

$$= 5 + \frac{0.031 \times 5 \times 10.19^2}{2 \times 9.81 \times 0.1} + \frac{10.19^2}{2 \times 9.81}$$

$$= 17.46 \text{ m of H}_2\text{O}$$

$$Q = AV_s$$

$$V_s = 10.19 \text{ m/s}$$

$$H_f = \frac{fLV^2}{2gD}$$

$$i) H_{md} = H_d + H_{fd} + \frac{V_d^2}{2g} - \frac{V_s^2}{2g}$$

$$= 6 + \frac{0.031 \times 6 \times 15.92^2}{2 \times 9.81 \times 0.08}$$

$$+ \frac{15.92^2}{2 \times 9.81} - \frac{10.19^2}{2 \times 9.81}$$

$$V_d = \frac{0.03}{\frac{\pi \times 0.08^2}{4}}$$

$$V_d = 15.92$$



$$\begin{aligned}
 g) \quad H_m &= H_s + H_d + H_{fs} + H_{fd} + \frac{V_0^2}{2g} \\
 &= 5 + 6 + \frac{0.031 \times 5 \times 10.19^2}{2 \times 9.81 \times 0.1} \\
 &\quad + \frac{0.031 \times 6 \times 15.92^2}{2 \times 9.81 \times 0.08} + \frac{15.92^2}{2 \times 9.81}
 \end{aligned}$$

$$H_m = 62.00 \text{ m}$$

d) Power

$$\begin{aligned}
 P &= \rho Q H_m \\
 &= 9810 \times 0.08 \times 62.00 \\
 &= 48.630 \text{ kW}
 \end{aligned}$$



Problem = 4       $(H_s)_{\max} = ?$

$$Q = 50 \text{ l/s} = 0.05 \text{ m}^3/\text{s}$$

$$D_s = 15 \text{ cm} = 0.15 \text{ m}$$

$$P_{\text{atm}} = 100 \text{ kN/m}^2 \text{ abs.}$$

$$P_{\text{vup}} = 2.34 \text{ kN/m}^2 \text{ abs.}$$

$$H_L = 2 \left( \frac{V_s^2}{2g} \right)$$

Sol:

$$\text{Area of the pipe} = \frac{Q}{V_s} = \frac{\pi D_s^2}{4} = 17.67 \times 10^{-3} \text{ m}^2$$

$$V_s = \frac{Q}{A_s} = 2.83 \text{ m/s}$$

$$\frac{V_s^2}{2g} = H_{vs} = 0.41 \text{ m of H}_2\text{O}$$

$$H_{ss} = 2 \left( \frac{V_s^2}{2g} \right) = 0.82 \text{ m of H}_2\text{O}$$

$$H_{\text{atm}} = \frac{P_{\text{atm}}}{\rho} = \frac{100 \times 10^3}{9810} = 10.19 \text{ m of H}_2\text{O}$$

$$H_{\text{vap}} = \frac{P_{\text{vap}}}{\rho} = \frac{2.34 \times 10^3}{9810} = 0.238 \text{ m of H}_2\text{O}$$

$$(H_{\text{max}}) = 10.19 - (0.238 + 0.41 + 0.82)$$
$$= 8.72 \text{ m of H}_2\text{O}$$

$$(H_{\text{max}}) = 28.35 \text{ ft of H}_2\text{O}$$



Daybook

14-1

Data

C.P

$$D_1 = 50 \text{ cm}$$

$$Q_1 = 3.2 \text{ m}^3/\text{s}$$

$$H_1 = 25 \text{ m}$$

$$N_1 = 1450 \text{ rpm}$$

a)  $\eta = 88\%$       BHP = ?

b) Homologous pump of

$$D_2 = 80 \text{ cm}$$

$$Q_2 = ?$$

Shaft Power = ?

$$N_2 = 1200 \text{ rpm}$$

$$H_2 = ?$$

Both pumps same efficiency.

c)  $N_s$  for both pumps = ?



Sol:

As  
a)

$$\eta = \frac{P_o}{P_{in}} \times 100$$

$$B.P = \frac{\rho g Q H}{\eta}$$

$$= \frac{9810 \times 3.2 \times 25}{0.88} = 9 \overset{57.07}{\cancel{20000}} \text{ kW.}$$

b)

$$\frac{Q_2}{Q_1} = \left(\frac{D_2}{D_1}\right)^3 \left(\frac{N_2}{N_1}\right)$$

$$\frac{Q_2}{3.2} = \left(\frac{0.8}{0.5}\right)^3 \left(\frac{1200}{1450}\right)$$

$$Q_2 = 10.85 \text{ m}^3/\text{s}$$

As

$$\frac{H_2}{H_1} = \left(\frac{D_2}{D_1}\right)^2 \left(\frac{N_2}{N_1}\right)^2$$

$$\frac{H_2}{25} = \left(\frac{0.8}{0.5}\right)^2 \left(\frac{1200}{1450}\right)^2$$

$$H_2 = 43.83 \text{ m}$$

As

$$\frac{P_2}{P_1} = \left(\frac{D_2}{D_1}\right)^5 \left(\frac{N_2}{N_1}\right)^3$$

$$\frac{P_2}{957.07} = \left(\frac{0.8}{0.5}\right)^5 \left(\frac{1200}{1450}\right)^3$$

$$P_2 = 5688 \text{ kW}$$



$$\begin{aligned} c) \quad N_{s1} &= \frac{N_1 \sqrt{Q_1}}{H_1^{3/4}} \\ &= \frac{1450 \sqrt{3.2}}{25^{3/4}} = 232 \end{aligned}$$

$$\begin{aligned} N_{s2} &= \frac{N_2 \sqrt{Q_2}}{H_2^{3/4}} \\ &= \frac{1200 \sqrt{10.85}}{43.83^{3/4}} = 232 \end{aligned}$$